

Suggested Solution for 2017 HKDSE Mathematics(core) Multiple Choice Questions

1. A

$$\begin{aligned} & 3m^2 - 5mn + 2n^2 + m - n \\ &= (3m - 2n)(m - n) + (m - n) \\ &= (m - n)(3m - 2n + 1) \end{aligned}$$

2. D

$$\begin{aligned} & \left(\frac{1}{9^{555}}\right)3^{444} \\ &= \left(\frac{1}{(3^2)^{555}}\right)3^{444} \\ &= \left(\frac{1}{3^{1110}}\right)3^{444} \\ &= \frac{1}{3^{666}} \end{aligned}$$

3. A

$$\begin{aligned} \frac{a+4b}{2a} &= 2 + \frac{b}{a} \\ \frac{a+4b}{2a} &= \frac{2a+b}{a} \\ a + 4b &= 2(2a + b) \\ a + 4b &= 4a + 2b \\ 3a &= 2b \\ a &= \frac{2b}{3} \end{aligned}$$

4. D

$$\begin{aligned} & \frac{1}{\pi^4} \\ & \approx 0.010265982 \\ & = 0.010266(\text{correct to 6 decimal places}) \end{aligned}$$

5. D

$$\begin{aligned} & 6 - x < 2x - 3 \text{ or } 7 - 3x > 1 \\ & 6 + 3 < 2x + x \text{ or } 7 - 1 > 3x \\ & 3x > 9 \text{ or } 3x < 6 \\ & x > 3 \text{ or } x < 2 \\ & \text{i.e. } x < 2 \text{ or } x > 3 \end{aligned}$$

6. A

$$\begin{aligned} f(2) - f(-2) \\ = 2(2)^2 - 5(2) + k - [2(-2)^2 - 5(-2) + k] \\ = -20 \end{aligned}$$

7. B

$$\begin{aligned} p(7) &= 0 \\ 2(7)^2 - 11(7) + c &= 0 \\ c &= -21 \\ \text{The remainder} \\ &= p\left(-\frac{1}{2}\right) \\ &= 2\left(-\frac{1}{2}\right)^2 - 11\left(-\frac{1}{2}\right) - 21 \\ &= -15 \end{aligned}$$

8. A

$$\begin{aligned} 4x^2 + m(x + 1) + 28 &\equiv mx(x + 3) + n(x - 4) \\ 4x^2 + mx + m + 28 &\equiv mx^2 + (3m + n)x - 4n \\ \text{By comparing coefficients of } x^2, \\ m &= 4 \\ \text{By comparing constant terms,} \\ -4n &= m + 28 \\ &= 4 + 28 \\ n &= -8 \end{aligned}$$

AlternativelyPut $x = 4$ on both sides,

$$\begin{aligned} 4(4)^2 + m(4 + 1) + 28 &= m(4)(4 + 3) + n(4 - 4) \\ m &= 4 \end{aligned}$$

Put $x = 0$ on both sides,

$$\begin{aligned} 4(0)^2 + 4(0 + 1) + 28 &= 4(0)(0 + 3) + n(0 - 4) \\ 32 &= -4n \\ n &= -8 \end{aligned}$$

9. C

$$\text{Vertex} = \left(-\frac{5}{p}, q\right)$$

From the graph,

$$-\frac{5}{p} < 0$$

$$p > 0 \text{ and } q < 0$$

10. C

Interest required

$$\begin{aligned} &= \$2\,000\left(1 + \frac{5\%}{2}\right)^{4 \times 2} - \$2\,000 \\ &= \$437 \text{(correct to the nearest dollar)} \end{aligned}$$

11. B

Let A be the actual area of the zoo.

$$\frac{4}{A} = \left(\frac{1}{20000}\right)^2$$

$$A = 1.6 \times 10^9 \text{ cm}^2$$

$$= 1.6 \times 10^5 \text{ m}^2$$

12. C

Let $y = k + k_1x^2$, where k and k_1 are constants.When $x = 1$, $y = 7$,

$$7 = k + k_1(1)^2 \text{ i.e. } k + k_1 = 7 \dots (1)$$

When $x = 2$, $y = 13$,

$$13 = k + k_1(2)^2 \text{ i.e. } k + 4k_1 = 13 \dots (2)$$

Solving (1) and (2),

$$k = 5 \text{ and } k_1 = 2$$

$$\therefore y = 5 + 2x^2$$

$$\text{When } x = 3, y = 5 + 2(3)^2$$

$$= 23$$

13. B

Let $T(n)$ be the number of dots in the n th pattern. Then,

$$T(1) = 1$$

$$T(2) = 1 + 2(1) + 2 = 5$$

$$T(3) = 5 + 2(2) + 2 = 11$$

$$T(4) = 11 + 2(3) + 2 = 19$$

$$T(5) = 19 + 2(4) + 2 = 29$$

$$T(6) = 29 + 2(5) + 2 = 41$$

$$T(7) = 41 + 2(6) + 2 = 55$$

14. B

Let $A \text{ cm}^2$ be the area of $\triangle BCD$. Then, the area of $\triangle ABD$ is $(A + 24) \text{ cm}^2$.

$$A + A + 24 = \frac{1}{2} \times 14 \times 12 = 84$$

$$A = 30$$

$$\text{Then, } \frac{1}{2} \times 12 \times DC = 30$$

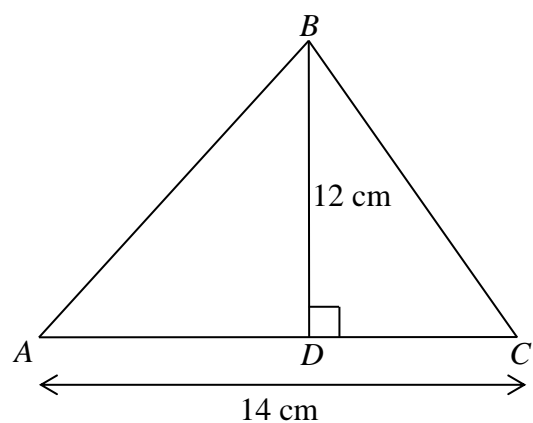
$$DC = 5 \text{ cm}$$

$$BC = \sqrt{12^2 + 5^2} = 13 \text{ cm}$$

$$AD = 14 - 5 = 9 \text{ cm}$$

$$AB = \sqrt{12^2 + 9^2} = 15 \text{ cm}$$

$$\text{Perimeter of } \triangle ABC = 13 + 14 + 15 = 42 \text{ cm}$$



15. C

Let r cm be the base radius of the right circular cylinder and h cm be the height of the right circular cone.

$$\frac{1}{3}\pi(2r)^2h = 36\pi$$

$$r^2h = 27$$

\therefore Volume of the circular cylinder

$$= \pi r^2(3h)$$

$$= 3\pi r^2h$$

$$= 3\pi(27)$$

$$= 81\pi \text{ cm}^3$$

16. D

By symmetry,

Area of $DFGH$ = area of $BEHG$

$$\therefore BE : EC = 2 : 3$$

$$\therefore GH : HC = 2 : 3 \text{ (intercept theorem)}$$

and $DF : FA = BE : EC = 2 : 3$ (by symmetry)

$$\therefore HG : GA = DF : FA = 2 : 3 \text{ (intercept theorem)}$$

Then, $AG : GC = 3 : (2 + 3) = 3 : 5$

Area of $\triangle CBG$: area of $\triangle ABG = GC : AG = 5 : 3$ ($\because \triangle CBG$ and $\triangle ABG$ have the same height.)

Area of $\triangle CBG$: 135 = 5 : 3

$$\text{Area of } \triangle CBG = 225 \text{ cm}^2$$

Note that $\triangle CEH \sim \triangle CBG$.

$$\therefore \frac{\text{Area of } \triangle CEH}{\text{Area of } \triangle CBG} = \left(\frac{CE}{CB}\right)^2$$

$$\text{i.e. } \frac{\text{Area of } \triangle CEH}{225} = \left(\frac{3}{3+2}\right)^2$$

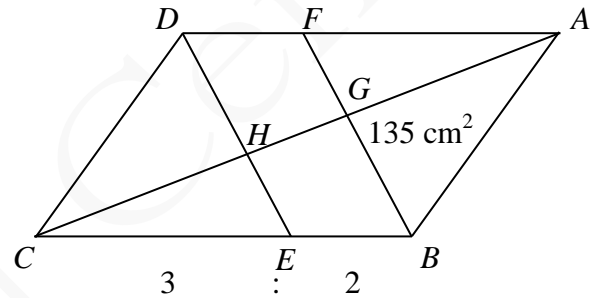
$$\therefore \text{Area of } \triangle CEH = 81 \text{ cm}^2$$

$$\therefore \text{Area of } BEHG = \text{Area of } \triangle CBG - \text{Area of } \triangle CEH$$

$$= 225 - 81$$

$$= 144 \text{ cm}^2$$

$$\text{i.e. Area of } DFGH = 144 \text{ cm}^2$$



17. D

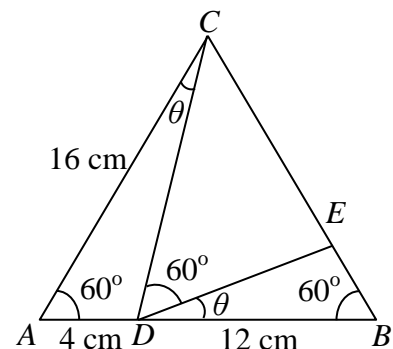
Note that $\triangle CAD \sim \triangle DBE$ and $DB = 12$ cm. Then,

$$\frac{BE}{AD} = \frac{DB}{CA} \text{ (corr. sides, } \sim \triangle\text{s)}$$

$$\frac{BE}{4} = \frac{12}{16}$$

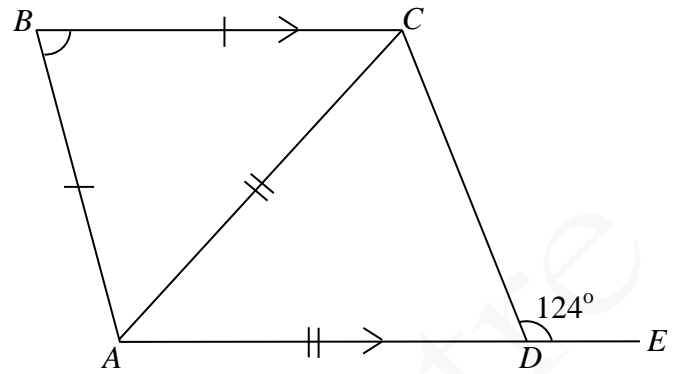
$$BE = 3 \text{ cm}$$

$$CE = CB - BE = 16 - 3 = 13 \text{ cm}$$



18. A

$$\begin{aligned} \angle CDA &= 180^\circ - 124^\circ \text{ (adj. } \angle \text{s on st. line)} \\ &= 56^\circ \\ \angle DCA &= \angle CDA \text{ (base } \angle \text{s, isos. } \triangle) \\ &= 56^\circ \\ \angle CAD + \angle CDA + \angle DCA &= 180^\circ \text{ (} \angle \text{ sum of } \triangle) \\ \angle CAD + 56^\circ + 56^\circ &= 180^\circ \\ \angle CAD &= 68^\circ \\ \angle BCA &= \angle CAD \text{ (alt. } \angle \text{s, } AE \parallel BC) \\ &= 68^\circ \\ \angle BAC &= \angle BCA \text{ (base } \angle \text{s, isos. } \triangle) \\ &= 68^\circ \\ \angle ABC + 68^\circ + 68^\circ &= 180^\circ \text{ (} \angle \text{ sum of } \triangle) \\ \angle ABC &= 44^\circ \end{aligned}$$



19. D

Vertical distance between A and H, y'

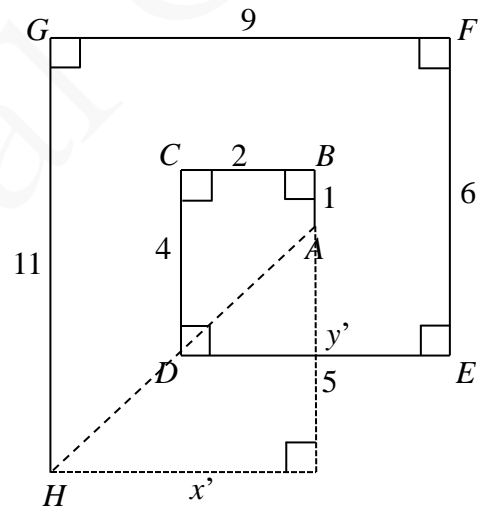
$$\begin{aligned} &= (11 - 6) + (4 - 1) \\ &= 8 \end{aligned}$$

Horizontal distance between A and H, x'

$$\begin{aligned} &= (9 - 5) + 2 \\ &= 6 \end{aligned}$$

By Pythagoras' theorem,

$$\begin{aligned} AH &= \sqrt{8^2 + 6^2} \\ &= 10 \end{aligned}$$



20. D

Without loss of generality, ABCD is drawn as shown.

$$\begin{aligned} \angle BDE &= \angle CBD \text{ (alt. } \angle \text{s, } BC \parallel AD) \\ EB = ED &\text{ (sides opp. equal } \angle \text{s)} \\ \angle BAE &= \angle ABE \text{ (base } \angle \text{s, isos. } \triangle) \\ &= \angle BDE \end{aligned}$$

Then, $AB = BD$ (sides opp. equal \angle s)

\therefore I is true.

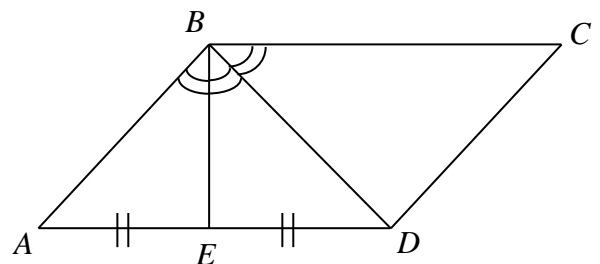
$\triangle ABE \cong \triangle DBE$ (SSS)

\therefore III is true.

$$\begin{aligned} \angle BEA &= \angle BED = 90^\circ \text{ (adj. } \angle \text{s on st. line)} \\ \angle ABE + \angle BAE + \angle BEA &= 180^\circ \text{ (} \angle \text{ sum of } \triangle) \\ \therefore \angle ABE &= \angle BAE = 45^\circ \end{aligned}$$

$$\angle ABC = \angle ABE + \angle DBE + \angle CBD = 45^\circ + 45^\circ + 45^\circ = 135^\circ$$

\therefore II is true.



21. C

Join BD .

$$\angle ABD = 90^\circ \text{ (}\angle \text{ in semi-circle)}$$

$$\angle CBD = \angle ABC - \angle ABD$$

$$= 110^\circ - 90^\circ$$

$$= 20^\circ$$

$$\angle CDB = \angle CBD \text{ (base } \angle \text{s, isos. } \triangle)$$

$$= 20^\circ$$

$$(*) \angle BCD + \angle CBD + \angle CDB = 180^\circ \text{ (}\angle \text{ sum of } \triangle)$$

$$\angle BCD + 20^\circ + 20^\circ = 180^\circ$$

$$\angle BCD = 140^\circ$$

$$\angle BED + \angle BCD = 180^\circ \text{ (opp. } \angle \text{s, cyclic quad.)}$$

$$\angle BED + 140^\circ = 180^\circ$$

$$\angle BED = 40^\circ$$

Alternatively

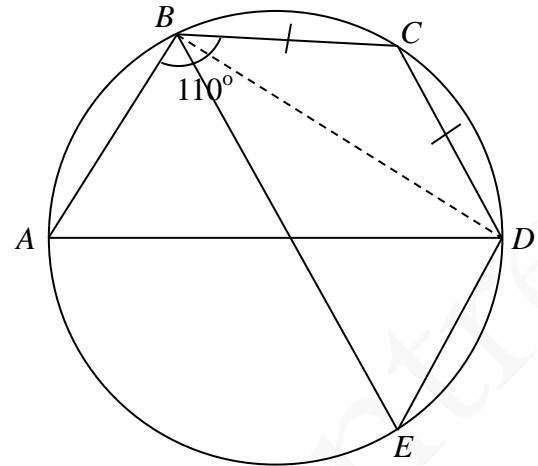
$$\widehat{BC} = \widehat{CD} \text{ (equal chords, equal arcs)}$$

$$\widehat{BC} : \widehat{BD} = 1 : 2$$

$$\angle BED : \angle BDC = 2 : 1 \text{ (arcs prop. to } \angle \text{s at } \odot^{\text{ce}})$$

$$\angle BED : 20^\circ = 2 : 1$$

$$\angle BED = 40^\circ$$



22. D

$$\tan 40^\circ = \frac{EC}{2}$$

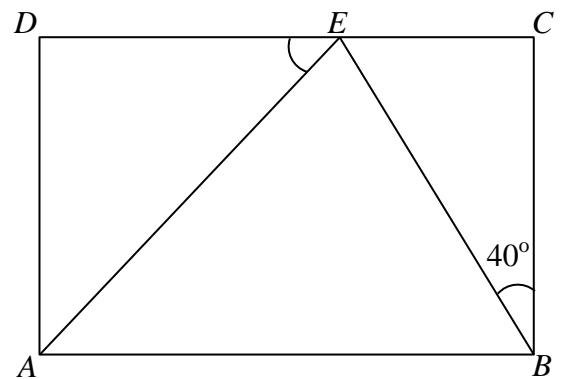
$$EC = 2 \tan 40^\circ \text{ cm}$$

$$\text{Then, } DE = (3 - 2 \tan 40^\circ) \text{ cm}$$

$$\therefore \tan \angle AED = \frac{AD}{DE}$$

$$= \frac{2}{3 - 2 \tan 40^\circ}$$

$$\therefore \angle AED \approx 57^\circ \text{ (correct to the nearest degree)}$$



23. A

x -intercept of $L_1 = n$ and x -intercept of $L_2 = q$.

From the graphs, $n > 0 > q \dots (1)$

\therefore II is true.

Rewrite $L_1 : y = -\frac{1}{m}x + \frac{n}{m}$ and $L_2 : y = -\frac{1}{p}x + \frac{q}{p}$.

y -intercept of $L_1 = \frac{n}{m}$ and y -intercept of $L_2 = \frac{q}{p}$

From the graphs, $\frac{n}{m} = -1$ i.e. $n + m = 0$

$\therefore n > 0$ [From (1)]

$\therefore m < 0 \dots (2)$

From the graphs, $\frac{q}{p} > 0$

$\therefore q < 0$ [From (1)]

$\therefore p < 0 \dots (3)$

$\therefore p + q < 0 = n + m$

\therefore III is NOT true.

Slope of $L_1 = -\frac{1}{m}$ and slope of $L_2 = -\frac{1}{p}$.

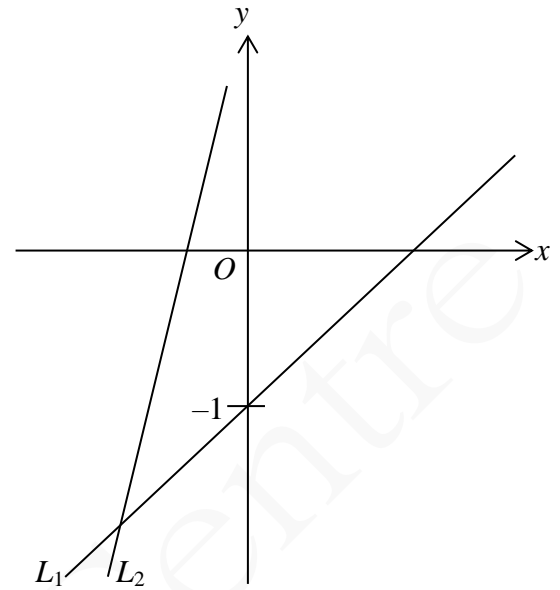
From the graphs, $-\frac{1}{p} > -\frac{1}{m}$

$$\frac{1}{p} < \frac{1}{m}$$

$\therefore m < 0$ and $p < 0$ [From (2) and (3)]

$\therefore m < p$

\therefore I is true.



24. A

Rewrite $y = \frac{9}{5}x + 9$ i.e. slope = $\frac{9}{5}$

Slope of $L = -1 \div \frac{9}{5} = -\frac{5}{9}$

Let the equation of L be $y = -\frac{5}{9}x + c$ where c is a constant.

Substitute $(-3, 0)$ into $y = -\frac{5}{9}x + c$,

$$0 = -\frac{5}{9}(-3) + c$$

$c = -\frac{5}{3} \therefore$ The required equation is $y = -\frac{5}{9}x - \frac{5}{3}$ i.e. $5x + 9y + 15 = 0$.

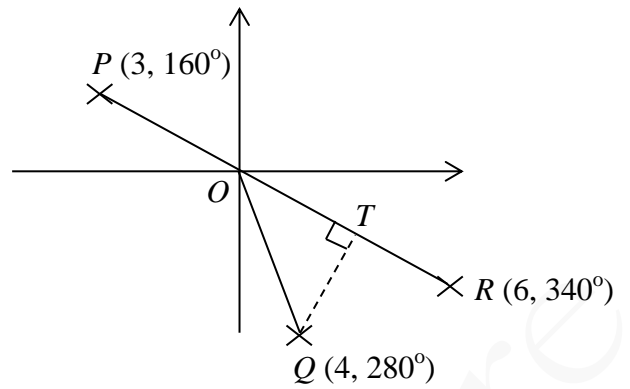
25. C

Let T be the foot of the perpendicular from Q to PR .Note that $\angle QOT = 60^\circ$.

$$\frac{QT}{OQ} = \sin \angle QOT$$

$$\frac{QT}{4} = \sin 60^\circ$$

$$QT = 2\sqrt{3}$$



26. A

Rewrite the equation of the circle C_2 as $x^2 + y^2 + 4x - 2y - \frac{5}{2} = 0$.

$$G_1 = (-4, 2), G_2 = (-2, 1)$$

Slope of $OG_1 = \frac{2}{-4} = -\frac{1}{2}$ and slope of $OG_2 = \frac{1}{-2} =$ slope of OG_1 $\therefore G_1, G_2$ and O are collinear. \therefore I is true.

$$\begin{aligned} \text{Radius of } C_1, r_1 &= \sqrt{(-4)^2 + (2)^2 - (-5)} \\ &= 5 \end{aligned}$$

$$\begin{aligned} \text{Radius of } C_2, r_2 &= \sqrt{(-2)^2 + (1)^2 - (-\frac{5}{2})} \\ &= \sqrt{\frac{15}{2}} \neq r_1 \end{aligned}$$

 \therefore II is NOT true.

$$\begin{aligned} OG_1 &= \sqrt{(-4)^2 + (2)^2} \\ &= \sqrt{20} \end{aligned}$$

$$\begin{aligned} OG_2 &= \sqrt{(-2)^2 + (1)^2} \\ &= \sqrt{5} \\ &\neq OG_1 \end{aligned}$$

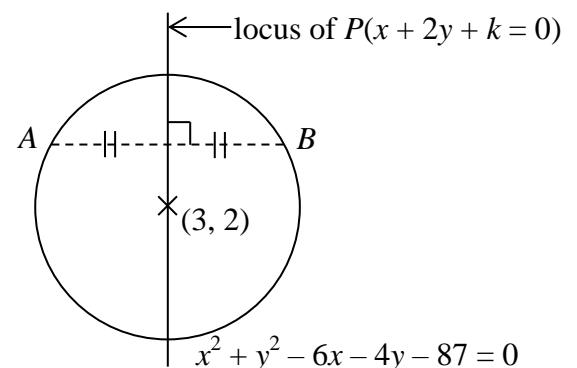
 \therefore III is NOT true.

27. B

Note that the locus of P is the perpendicular bisector of AB and passes through the centre of the circle.Centre of the circle = $(3, 2)$

$$\therefore (3) + 2(2) + k = 0$$

$$k = -7$$



28. C

Number of favourable outcomes = $5 + 20 = 25$ Number of possible outcomes = $5 + 20 + 15 + 10 + 10 = 60$

$$\begin{aligned}\therefore \text{The required probability} &= \frac{25}{60} \\ &= \frac{5}{12}\end{aligned}$$

29. B

The lower quartile = the lower end of the box = 15

30. B

 \therefore Mean = 5

$$\therefore \frac{2+3+4+6+7+9+10+m+n}{9} = 5$$

i.e. $m + n = 4$ When $m = 1$ and $n = 3$, $a = 3$, $b = 4$ and $c = 10 - 1 = 9$.When $m = 2$ and $n = 2$, $a = 2$, $b = 4$ and $c = 10 - 2 = 8$. \therefore Only $b = 4$ must be true.

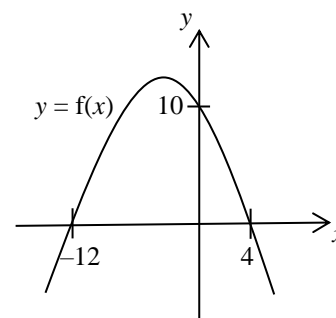
31. D

Note that $g(x) = f\left(\frac{x}{2}\right)$ represents an enlargement of 2 times along the x -axis. The answer is D.AlternativelyFrom the graph of $f(x)$, $f(0) = 10$, $f(-12) = f(4) = 0$

$$\therefore g(x) = f\left(\frac{x}{2}\right)$$

$$\therefore g(0) = f\left(\frac{0}{2}\right) = f(0) = 10 \quad \text{i.e. The } y\text{-intercept of } g(x) \text{ is } 10.$$

$$g(-24) = f\left(\frac{-24}{2}\right) = f(-12) = 0 \quad \text{and} \quad g(8) = f\left(\frac{8}{2}\right) = f(4) = 0 \quad \text{i.e. The } x\text{-intercepts of } g(x) \text{ are } -24 \text{ and } 8.$$



32. D

Note that $8^3 = 2(16^2)$ and $8^4 = 16^3$.

$$\begin{aligned}
 &8^3 + 8^{19} \\
 &= 8^3(1 + 8^{16}) \\
 &= 2(16^2)[1 + (8^4)^4] \\
 &= 2(16^2)[1 + (16^3)^4] \\
 &= 2(16^2)(1 + 16^{12}) \\
 &= 2(16^2) + 2(16^{14}) \\
 &= 200000000000200_{16}
 \end{aligned}$$

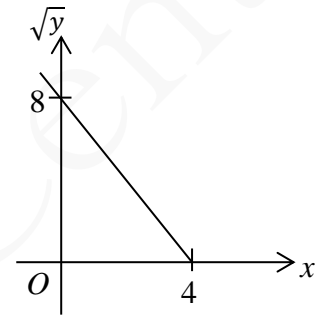
16^{14}	16^{13}	16^{12}	16^{11}	16^{10}	16^9	16^8	16^7	16^6	16^5	16^4	16^3	16^2	16^1	16^0
2	0	0	0	0	0	0	0	0	0	0	0	2	0	0

33. C

Slope of the graph = -2 and \sqrt{y} -intercept of the graph = 8

Equation of the straight line is

$$\begin{aligned}
 \sqrt{y} &= -2x + 8 \\
 y &= (-2x + 8)^2 \\
 &= 4x^2 - 32x + 64
 \end{aligned}$$



34. D

$$\begin{cases}
 \log_9 y = x - 3 & \text{i.e. } x = \log_9 y + 3 \dots (1) \\
 2(\log_9 y)^2 = 4 - x \dots (2)
 \end{cases}$$

Substitute (1) into (2),

$$\begin{aligned}
 2(\log_9 y)^2 &= 4 - (\log_9 y + 3) \\
 2(\log_9 y)^2 &= 4 - \log_9 y - 3 \\
 2(\log_9 y)^2 + \log_9 y - 1 &= 0 \\
 (2\log_9 y - 1)(\log_9 y + 1) &= 0
 \end{aligned}$$

$$\log_9 y = \frac{1}{2} \text{ or } -1$$

$$y = 3 \text{ or } \frac{1}{9}$$

35. B

$$\begin{aligned}
 &\frac{5}{2-i} + ki \\
 &= \frac{5(2+i)}{(2-i)(2+i)} + ki
 \end{aligned}$$

$$= \frac{10+5i}{2^2-i^2} + ki$$

$$= 2 + (k+1)i$$

 \therefore The number is a real number.

$$\therefore k + 1 = 0$$

$$k = -1$$

36. C

$$\pi^{45} - \pi^{30} \neq \pi^{60} - \pi^{45}$$

\therefore I is NOT an arithmetic sequence.

$$45\pi - 30\pi = 60\pi - 45\pi = 15\pi$$

\therefore II is an arithmetic sequence.

$$(\pi - 45) - (\pi - 30) = (\pi - 60) - (\pi - 45) = -15$$

\therefore III is an arithmetic sequence.

37. C

Draw the straight lines of $y = 9$, $x - y - 9 = 0$ and $x + y - 9 = 0$.

The points of intersections are $(0, 9)$, $(9, 0)$ and $(18, 9)$.

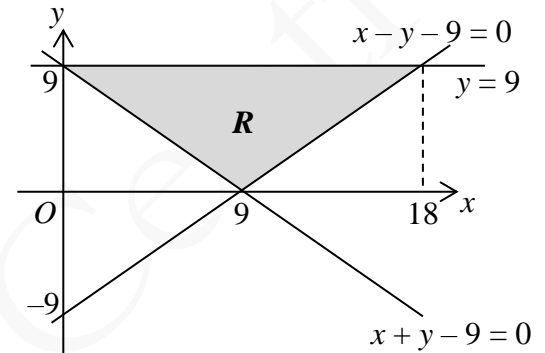
Let $P = x - 2y + 43$.

$$P(0, 9) = (0) - 2(9) + 43 = 25$$

$$P(9, 0) = (9) - 2(0) + 43 = 52$$

$$P(18, 9) = (18) - 2(9) + 43 = 43$$

\therefore The greatest value of $x - 2y + 43$ is 52.



38. A

By Pythagoras' theorem,

$$\begin{aligned} AC &= \sqrt{AB^2 + BC^2} \\ &= \sqrt{28^2 + 21^2} \\ &= 35 \text{ cm} \end{aligned}$$

$$\begin{aligned} EC &= AC - AE \\ &= 35 - 30 \\ &= 5 \text{ cm} \end{aligned}$$

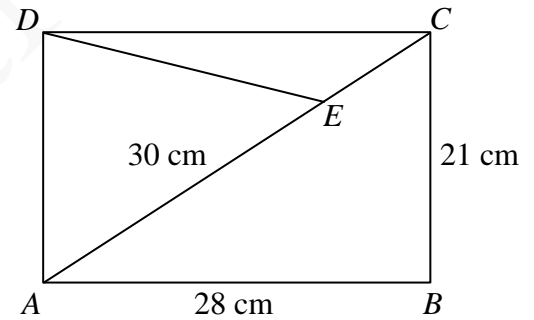
$$\cos \angle BAC = \frac{AB}{AC} = \frac{28}{35} = \frac{4}{5}$$

Note that $\angle DCA = \angle BAC$ (alt. \angle s, $AB \parallel DC$)

$$\therefore \cos \angle DCA = \cos \angle BAC = \frac{4}{5}$$

By cosine formula,

$$\begin{aligned} DE^2 &= CD^2 + EC^2 - 2(CD)(EC)\cos \angle DCA \\ &= 28^2 + 5^2 - 2(28)(5)\left(\frac{4}{5}\right) \\ &= 585 \\ DE &= \sqrt{585} \\ &= 3\sqrt{65} \text{ cm} \end{aligned}$$



Alternatively

$$\cos \angle BCA = \frac{BC}{AC} = \frac{21}{35} = \frac{3}{5}$$

Note that $\angle DAC = \angle BCA$ (alt. \angle s, $AD \parallel BC$)

$$\therefore \cos \angle DAC = \cos \angle BCA = \frac{3}{5}$$

By cosine formula,

$$\begin{aligned} DE^2 &= AD^2 + AE^2 - 2(AD)(AE)\cos \angle DAC \\ &= 21^2 + 30^2 - 2(21)(30)\left(\frac{3}{5}\right) \\ &= 585 \\ DE &= \sqrt{585} \\ &= 3\sqrt{65} \text{ cm} \end{aligned}$$

39. A

By Pythagoras' theorem,

$$BD^2 + AD^2 = AB^2$$

$$BD^2 + 15^2 = 25^2$$

$$BD = 20 \text{ m}$$

$$BD^2 + CD^2 = 20^2 + 21^2$$

$$= 29^2$$

$$= BC^2$$

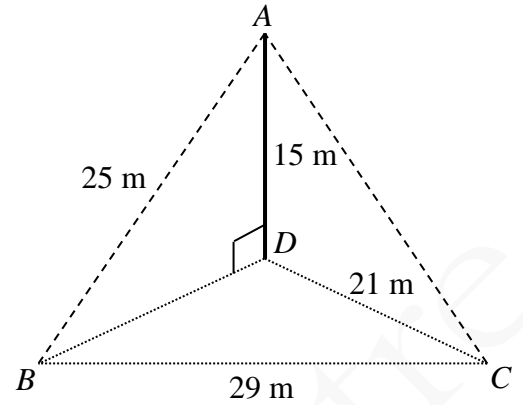
∴ $\triangle BCD$ is a right-angled \triangle with $\angle BDC = 90^\circ$.

i.e. Plane ABD is perpendicular to plane ADC .

The projection of AB on plane ADC is AD . The required angle is $\angle BAD$. Then,

$$\tan \angle BAD = \frac{20}{15} \quad / \sin \angle BAD = \frac{20}{25} \quad / \cos \angle BAD = \frac{15}{25}$$

∴ $\angle BAD = 53^\circ$ (correct to the nearest degree)



40. B

$$\angle OAD = 90^\circ \text{ (tangent } \perp \text{ radius)}$$

$$\angle OAB = \angle OAD - \angle BAD$$

$$= 90^\circ - 68^\circ$$

$$= 22^\circ$$

Join BO .

$$\angle OBA = \angle OAB \text{ (base } \angle \text{s, isos. } \triangle)$$

$$= 22^\circ$$

$$\angle CBO = \angle BCO \text{ (base } \angle \text{s, isos. } \triangle)$$

$$= 26^\circ$$

$$\angle ABC = \angle CBO + \angle OBA$$

$$= 26^\circ + 22^\circ$$

$$= 48^\circ$$

Alternatively

Join AC .

$$\angle ACB = \angle BAD \text{ (} \angle \text{ in alt. segment)}$$

$$= 68^\circ$$

$$\angle OCA = \angle ACB - \angle BCO$$

$$= 68^\circ - 26^\circ$$

$$= 42^\circ$$

$$\angle OAC = \angle OCA \text{ (base } \angle \text{s, isos. } \triangle)$$

$$= 42^\circ$$

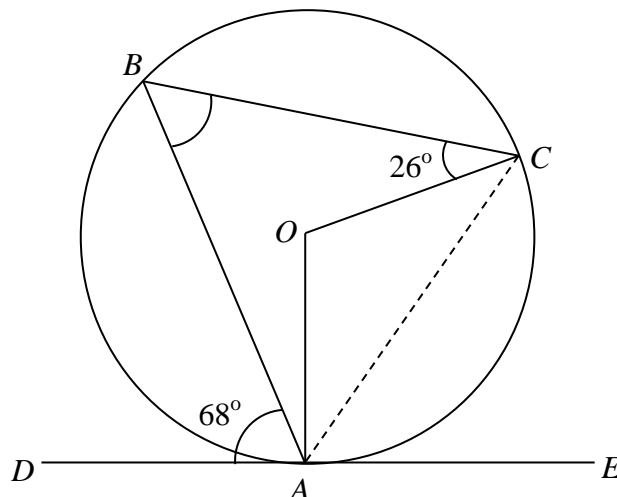
$$\angle AOC + \angle OAC + \angle OCA = 180^\circ \text{ (} \angle \text{ sum of } \triangle)$$

$$\angle AOC + 42^\circ + 42^\circ = 180^\circ$$

$$\angle AOC = 96^\circ$$

$$\angle ABC = \frac{1}{2} \angle AOC \text{ (} \angle \text{ at centre twice } \angle \text{ at } \odot^{\text{ce}})$$

$$= 48^\circ$$



41. D

Let $G(a, a)$ be the in-centre of $\triangle OPQ$ and A, B and C be the tangent points to the circle inscribed in $\triangle OPQ$ on the y -axis, the x -axis and PQ respectively. Then,

$$3a + 4a = 3p$$

$$a = \frac{3}{7}p$$

$$OA = OB = a = \frac{3}{7}p \text{ (tangent properties)}$$

$$QC = QA = q - \frac{3}{7}p \text{ (tangent properties)}$$

$$\begin{aligned} CP = BP &= p - \frac{3}{7}p \text{ (tangent properties)} \\ &= \frac{4}{7}p \end{aligned}$$

$$GC = a = \frac{3}{7}p$$

Note that $\triangle QAG \cong \triangle QCG$ and $\triangle PBG \cong \triangle PCG$.

Area of $\triangle OPQ$ = area of $AOBG$ + $2 \times$ area of $\triangle QAG$ + $2 \times$ area of $\triangle PBG$

$$\frac{1}{2}pq = \left(\frac{3}{7}p\right)\left(\frac{3}{7}p\right) + 2 \times \frac{1}{2} \times \left(q - \frac{3}{7}p\right)\left(\frac{3}{7}p\right) + 2 \times \frac{1}{2} \times \left(\frac{4}{7}p\right)\left(\frac{3}{7}p\right)$$

$$\frac{p}{q} = \frac{7}{24} \text{ i.e. } p : q = 7 : 24$$

Alternatively

$$QP = QC + CP$$

$$QP^2 = (QC + CP)^2$$

$$p^2 + q^2 = \left(q - \frac{3}{7}p + \frac{4}{7}p\right)^2$$

$$p^2 + q^2 = q^2 + \frac{2}{7}pq + \frac{1}{49}p^2$$

$$\frac{p}{q} = \frac{7}{24} \text{ i.e. } p : q = 7 : 24$$

42. B

Number of teams formed

$$= C_5^{13} \times C_4^6$$

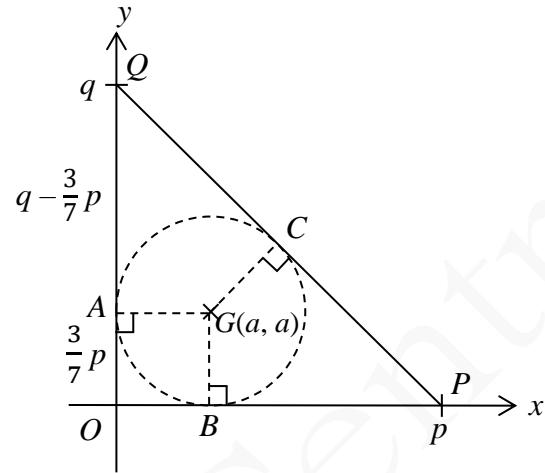
$$= 19\,305$$

43. C

The required probability = $1 - P(\text{"she hits the target 4 times"})$

$$= 1 - (0.7)^4$$

$$= 0.7599$$



44. B

Let σ be the standard deviation of the test scores. Then,

$$\frac{33-45}{\sigma} = -2$$

$$\sigma = 6$$

\therefore The standard deviation of the scores is 6 marks.

45. A

As all data are increased to 8 times the original ones, the new mode is increased to 8 times the original one as well.

\therefore I is true.

As all data are increased to 8 times the original ones, the new inter-quartile range is increased to 8 times the original one as well.

\therefore II is true.

As all data are increased to 8 times the original ones, the new variance is increased to 64 times the original one.

\therefore III is NOT true.